

Calculus DIFFERENTIATION AND INTEGRATION Table (u = u(x))

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|---|---|
| 1. $D_x(c) = 0$ | 1. $\int c \, dx = cx + C$ |
| 2. $D_x(c f(x)) = c D_x(f(x))$ | 2. $\int c f(x) \, dx = c \int f(x) \, dx$ |
| 3. $D_x(x^n) = n x^{n-1}$ | 3. $\int x^n \, dx = (x^{n+1}) / (n+1) + C \quad \text{for } n \neq -1$ |
| 4. $D_x(u^n) = n u^{n-1} u'(x)$ | 4. $\int u^n u' \, dx = \int u^n \, du = u^{n+1} / (n+1) + C \quad \text{for } n \neq -1$ |
| 5. $D_x(f \pm g) = f'(x) \pm g'(x)$ | 5. $\int (f \pm g) \, dx = \int f \, dx \pm \int g \, dx$ |
| 6. $D_x(f \cdot g) = f'(x) g(x) + g'(x) f(x)$ | 6. $\int \sin u \, du = -\cos u + C$ |
| 7. $D_x(f/g) = (f'(x) g(x) - g'(x) f(x)) / (g(x))^2$ | 7. $\int \cos u \, du = \sin u + C$ |
| 8. $D_x(f(u(x))) = (df/du)(du/dx) = f'(u) u'(x)$ | 8. $\int \sec^2 u \, du = \tan u + C$ |
| 9. $D_x(\sin u) = u'(x) \cos u$ | 9. $\int \csc^2 u \, du = -\cot u + C$ |
| 10. $D_x(\cos u) = -u'(x) \sin u$ | 10. $\int \csc u \cot u \, du = -\csc u + C$ |
| 11. $D_x(\tan u) = u'(x) \sec^2(u)$ | 11. $\int \sec u \tan u \, du = \sec u + C$ |
| 12. $D_x(\csc u) = -u'(x) \csc u \cot u$ | 12. $\int \sec u \, du = \ln \sec u + \tan u + C$ |
| 13. $D_x(\sec u) = u'(x) \sec u \tan u$ | 13. $\int \csc u \, du = \ln \csc u - \cot u + C$ |
| 14. $D_x(\cot u) = -u'(x) \csc^2 u$ | 14. $\int du/u = \ln u + C$ |
| 15. $D_x(e^u) = e^u u'(x)$ | 15. $\int e^u \, du = e^u + C$ |
| 16. $D_x(a^u) = a^u u'(x) \ln a$ | 16. $\int a^u u' \, dx = \int a^u \, du = \int e^u \ln a \, du = a^u / \ln a + C$ |
| 17. $D_x(\ln u) = u'(x) / u$ | 17. $\int \tan u \, du = -\ln \cos u + C \text{ or } \ln \sec u + C$ |
| 18. $D_x(\log_a u) = u'(x) / (u \ln a)$ | 18. $\int \cot u \, du = \ln \sin u + C$ |
| 19. $D_x(\arcsin u) = u'(x) / (1 - u^2)^{1/2}$ | 19. $\int \sin^2 u \, du = (1/2)(u - (\sin 2u)/2) + C$ |
| 20. $D_x(\arctan u) = u'(x) / (1 + u^2)$ | 20. $\int \cos^2 u \, du = (1/2)(u + (\sin 2u)/2) + C$ |
| 21. $D_x(\operatorname{arcsec} u) = u'(x) / (u(u^2 - 1)^{1/2})$ | 21. $\int \tan^2 u \, du = \tan u - u + C$ |
| 22. $D_x(\sinh u) =$ | 22. $\int \cot^2 u \, du = -\cot u - u + C$ |
| 23. $D_x(\cosh u) =$ | 23. $I \frac{du}{\sqrt{a^2 - u^2}} = \arcsin(u/a) + C$ |
| 24. $D_x(\tanh u) =$ | 24. $I \frac{du}{u \sqrt{u^2 - a^2}} = (1/a) \operatorname{arcsec}(u/a) + C$ |
| 25. $D_x(\operatorname{sech} u) =$ | 25. $I \frac{du}{a^2 + u^2} = (1/a) \operatorname{arc tan}(u/a) + C$ |
| 26. $D_x(\operatorname{csch} u) =$ | 26. $I \frac{P(x) \, dx}{Q(x)}, \deg P \geq \deg Q, \text{ use long division first}$ |
| 27. $D_x(\coth u)$ | 27. $I x^n \sqrt{ax + b} \, dx, \text{ let } u = ax + b$ |
| | 28. $I \frac{du}{\sqrt{au^2 + bu + c}}, \text{ use trig substitution}$ |